

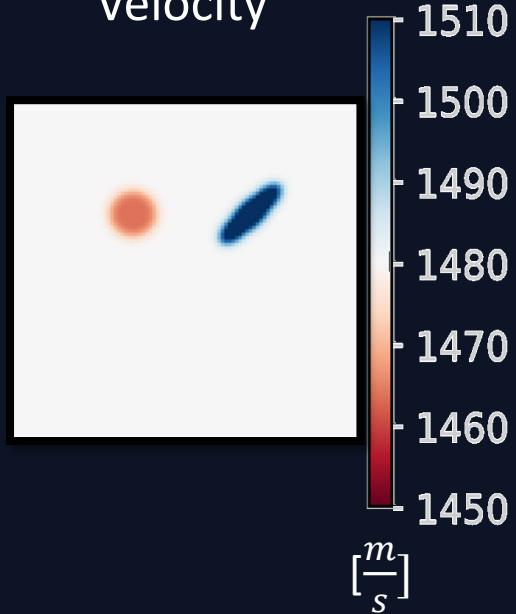
IMVC 2024

Model-Based Real Time Quantitative Ultrasound and Radar

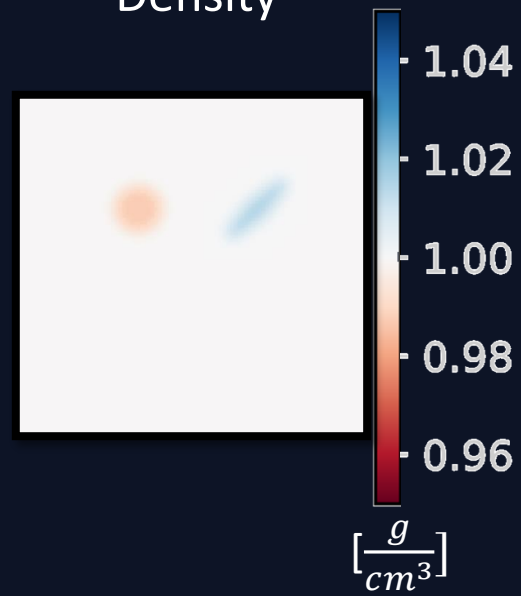
Tom Sharon, Yonina C. Eldar

Motivation

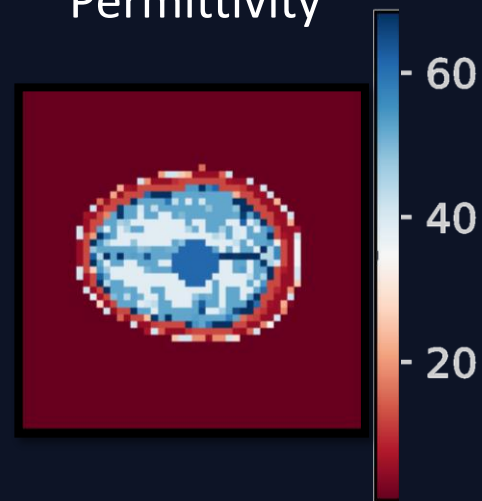
Velocity



Density



Permittivity



Conductivity



Motivation



Healthy liver



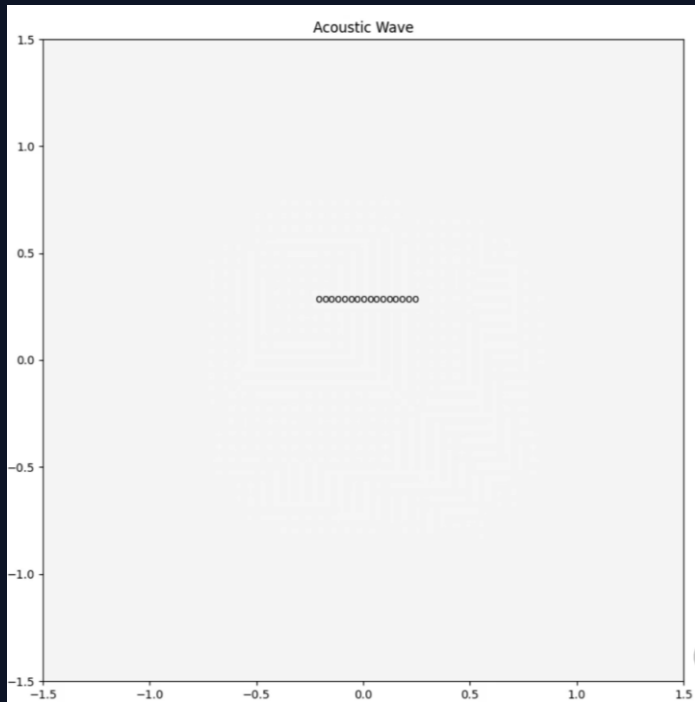
Fatty liver

Fat percentage [%]



Blood spread
over time?

Problem statements

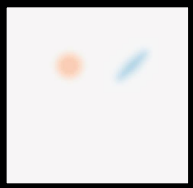
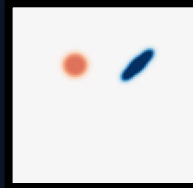


Forward Problem

US wave equation

Radar wave equation

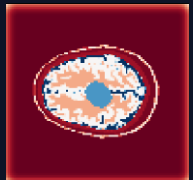

SoS density



US

Distinguish between benign and malignant tumors Estimate the fat % in the liver

permittivity conductivity

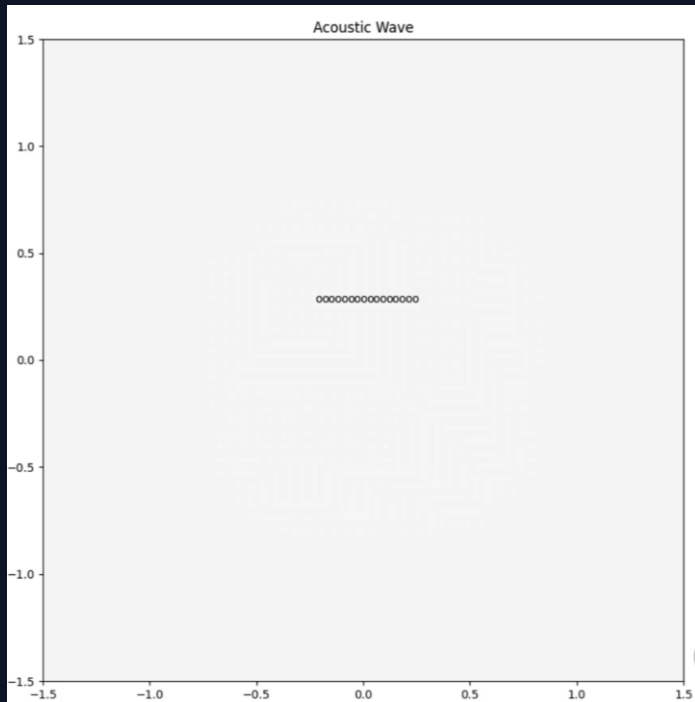


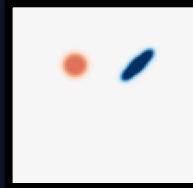
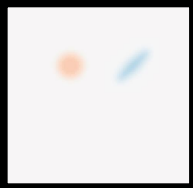

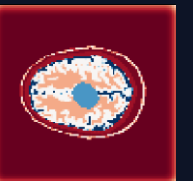
Radar

Show different organs or properties of the human body in different contrast

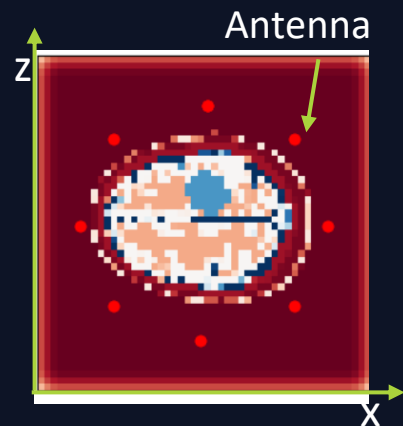
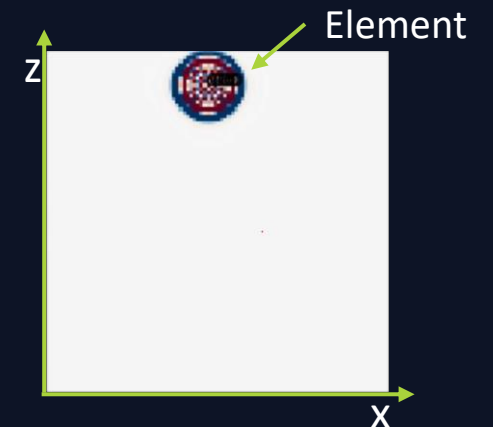
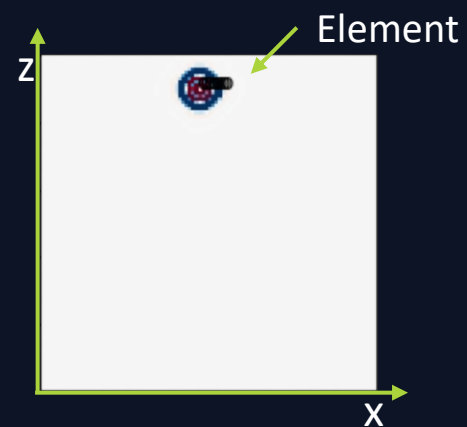
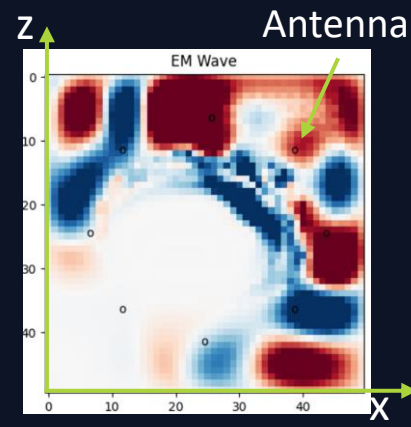
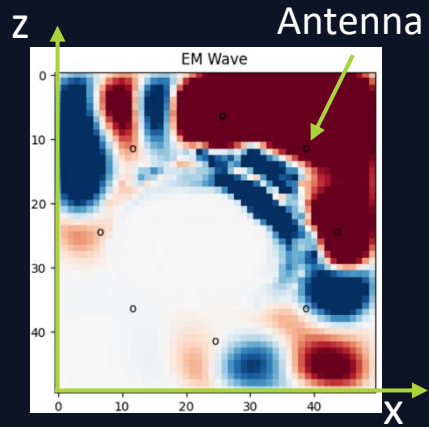
Blood spreading in Hemorrhagic stroke

Problem statements

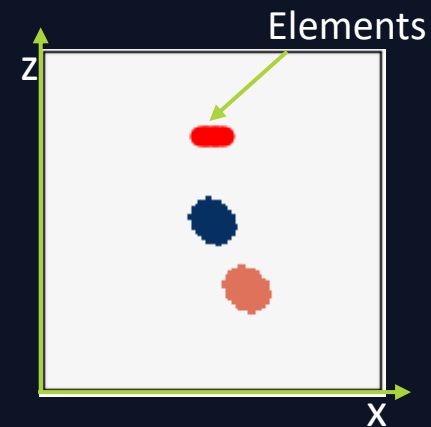


	SoS	density
		
	Distinguish between benign and malignant tumors	Estimate the fat % in the liver
	permittivity	conductivity
		
	Show different organs or properties of the human body in different contrast	
	Blood spreading in Hemorrhagic stroke	

Problem statements

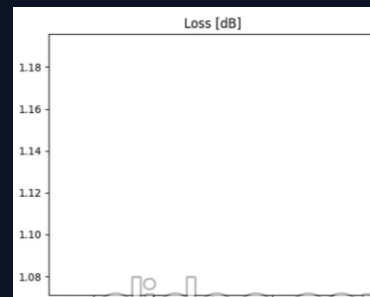
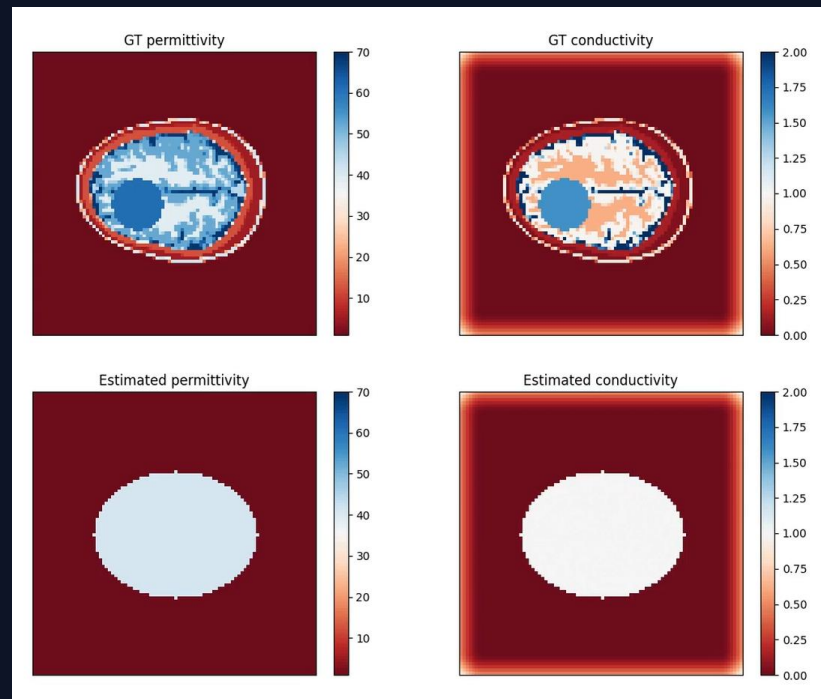


- 8 elements
- 1 transmits – the rest record



Full Waveform Inversion (FWI) algorithm

An iterative optimization method, based on GD, to achieve quantitative imaging from the signals



Advantages

- No training
- Recovers different physical properties

Disadvantages

- Time consuming
- Tends to converge to a local minima
- Initial guess should be close to true solution

Full Waveform Inversion (FWI) algorithm

An iterative optimization method, based on GD, to achieve quantitative imaging from the signals

$$L(\{\theta_j\}_{j=1}^{n_m}) = \frac{1}{2} \left\| M - F(\{\theta_j\}_{j=1}^{n_m}) \right\|_2^2$$

→ Predicted signals

The update of the physical property in the $i+1$ iteration:

$$\theta_j^{i+1} = \theta_j^i - \eta \frac{\partial L(\{\theta_j^i\}_{j=1}^{n_m})}{\partial \theta_j}$$

$\theta_j \in \mathbb{R}^{n_x \times n_z}$ is the j 'th physical property out of n_m properties

M is the measured signals

$F()$ is the known wave propagation equation

Data creation

MNIST

permittivity

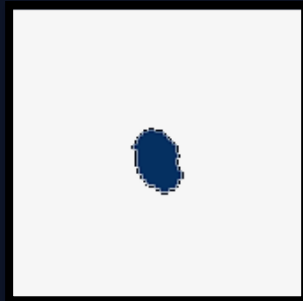


conductivity

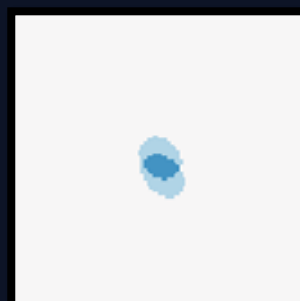


Overlapping ovals

SoS



density



Simulated scanned medium



Model F: Wave equation

Narrow pulse [ns]



Model-based deep learning

Better than
pure analytical
solution

- ✓ Improved inference results
- ✓ Improved inference time

Better than
standard deep
NN

- ✓ Requires less training data
- ✓ Better generalization

Our method: MB-QRUS

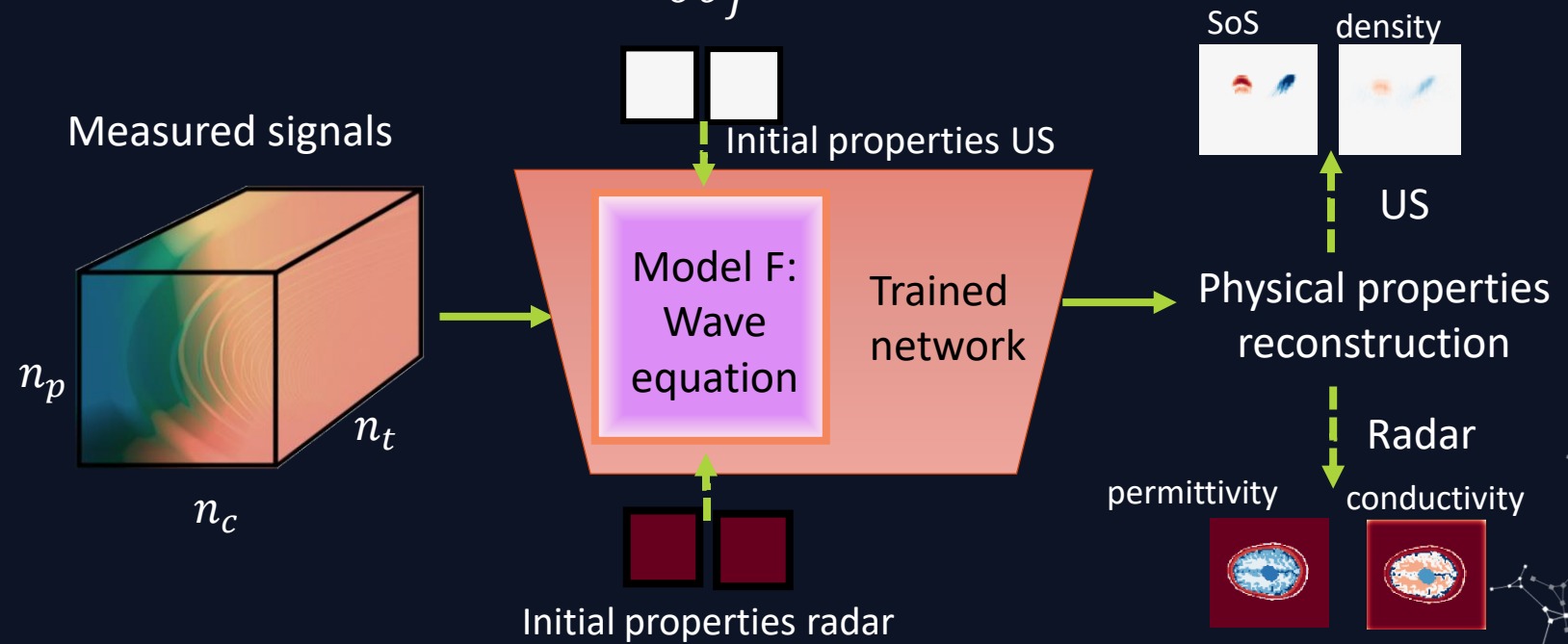
- Unfolding of FWI with learned gradients ($G = \frac{\partial L}{\partial \theta_j}$) according to a U-Net based block

- Network input:

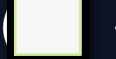
- M
- $\{\theta_j^0\}_{j=1}^{n_m}$

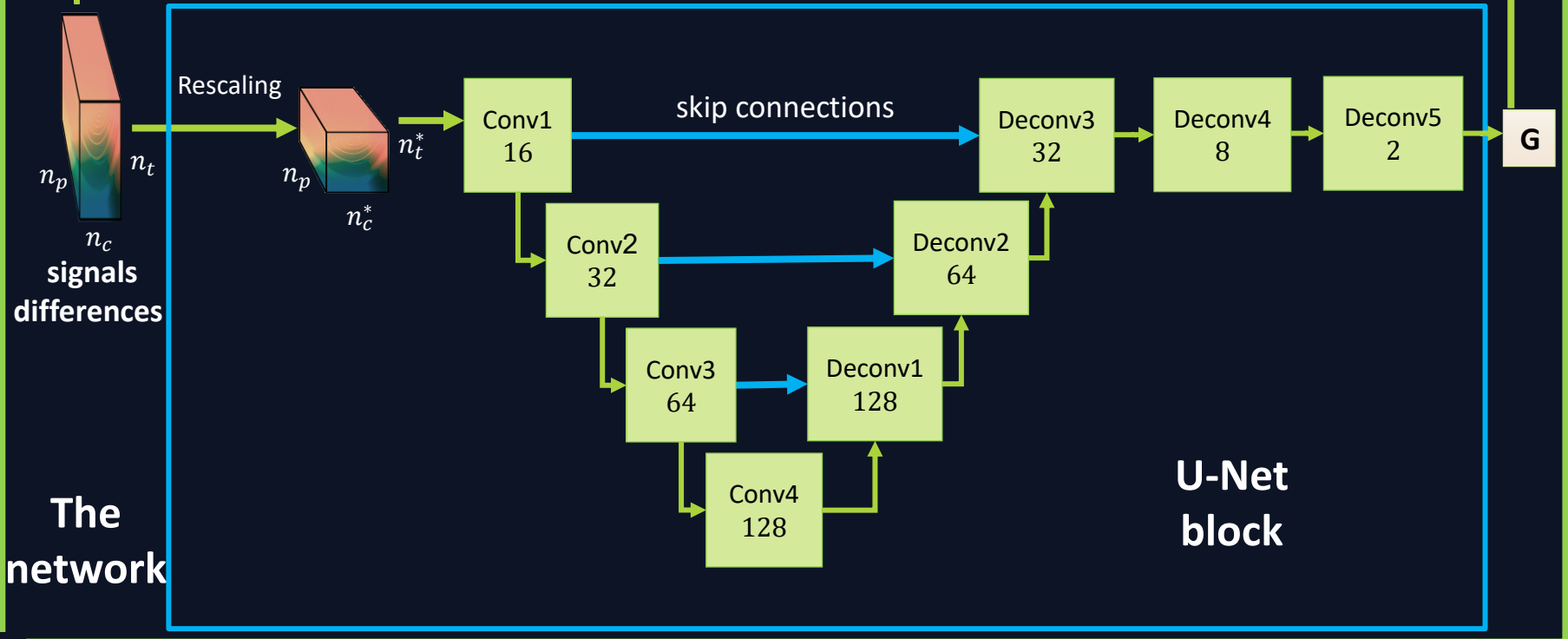
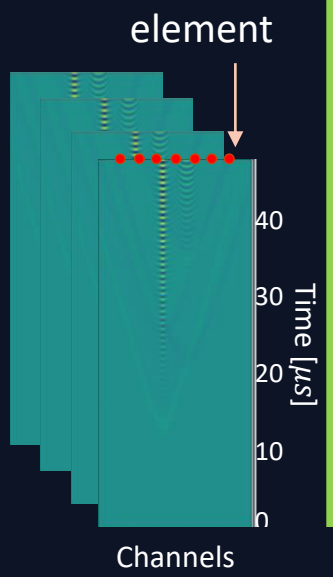
- Output:

- $\{\theta_j^L\}_{j=1}^{n_m}$





ReLU( -G)



The network



Results

$$NRMSE(\hat{\theta}) = \frac{\sqrt{\|\hat{\theta} - \theta_{GT}\|_F^2 / (n_x n_z)}}{\theta_{max} - \theta_{min}}$$



$$PSNR(\hat{\theta}) = 20 \log_{10} \theta_{max} - \log_{10} \|\hat{\theta} - \theta_{GT}\|_F^2$$



$$SSIM(x, y) = \frac{(2\mu_x\mu_y + c_1)(2\sigma_{xy} + c_2)}{(\mu_x^2 + \mu_y^2 + c_1)(\sigma_x^2 + \sigma_y^2 + c_2)}$$



MNIST '0'

Noisy Medium

Noisy input

Two Objects

Linear Probe

SoS

density

SoS

density

SoS

density

SoS

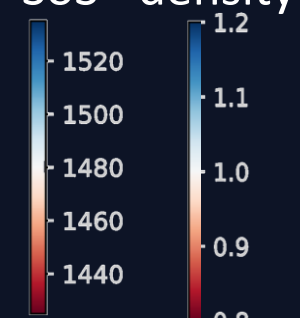
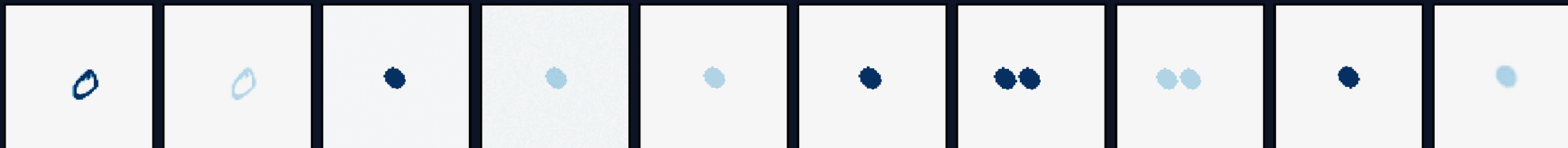
density

SoS

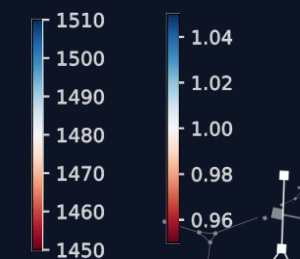
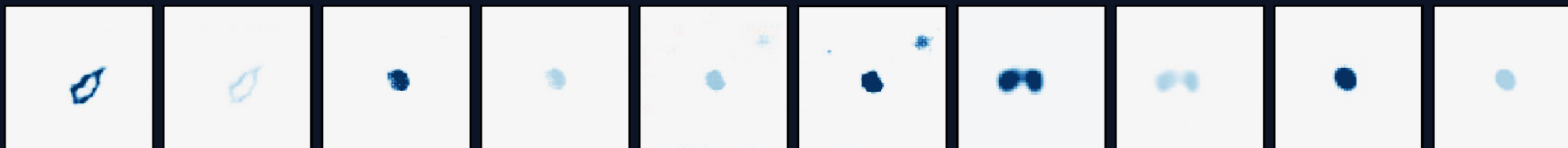
density

SoS density

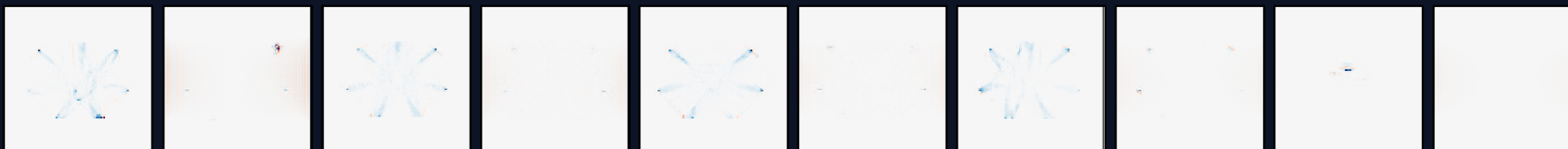
GT



Ours



FWI

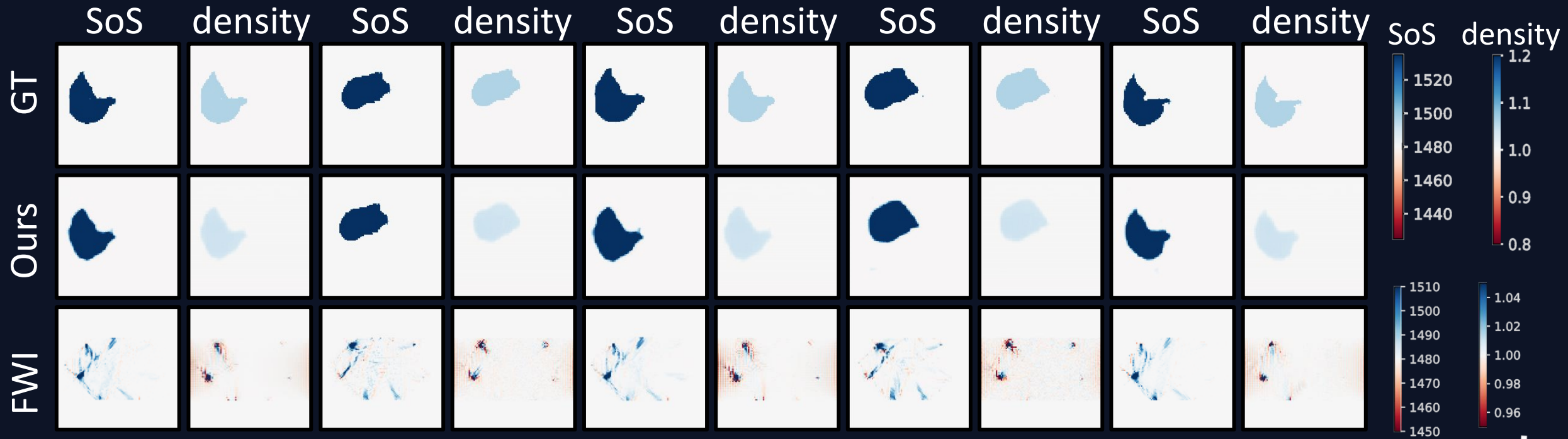


Property	NRMSE	PSNR	SSIM
SoS	-56.33%	1.93%	8.15%
density	-55.43%	13.15%	6.10%

OURS	FWI
< 1 second	> 32 minutes



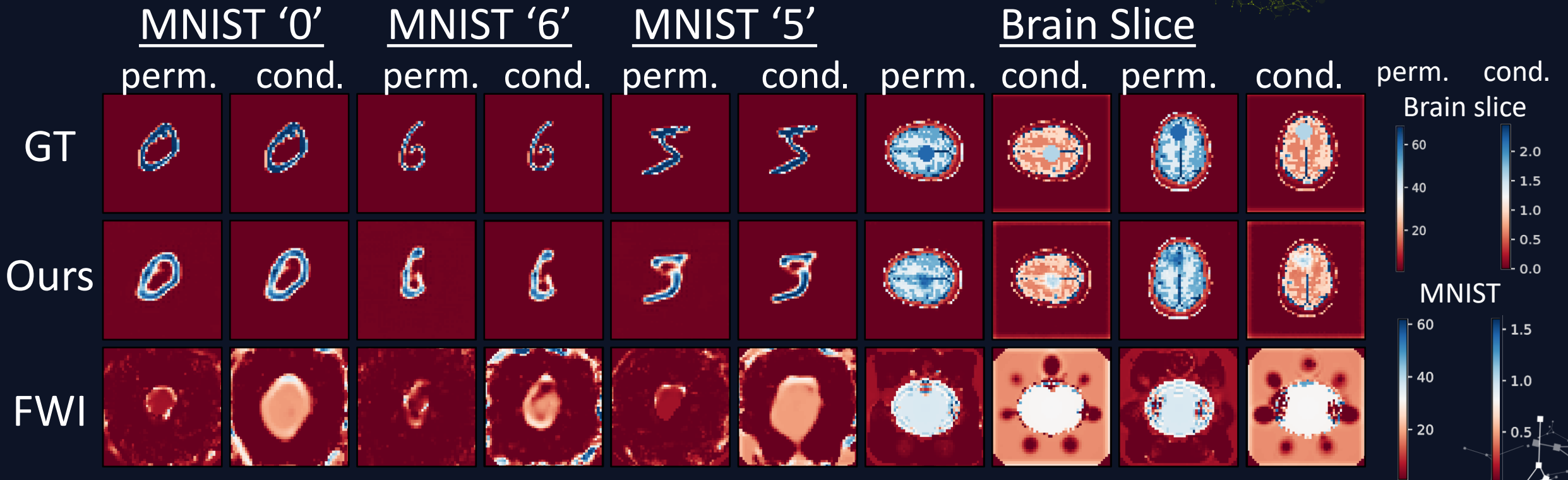
Realistic liver shapes



Property	NRMSE	PSNR	SSIM
SoS	-62.87%	1.7%	20.72%
density	-62.35%	53.37%	33.63%

OURS	FWI
< 1 second	> 32 minutes



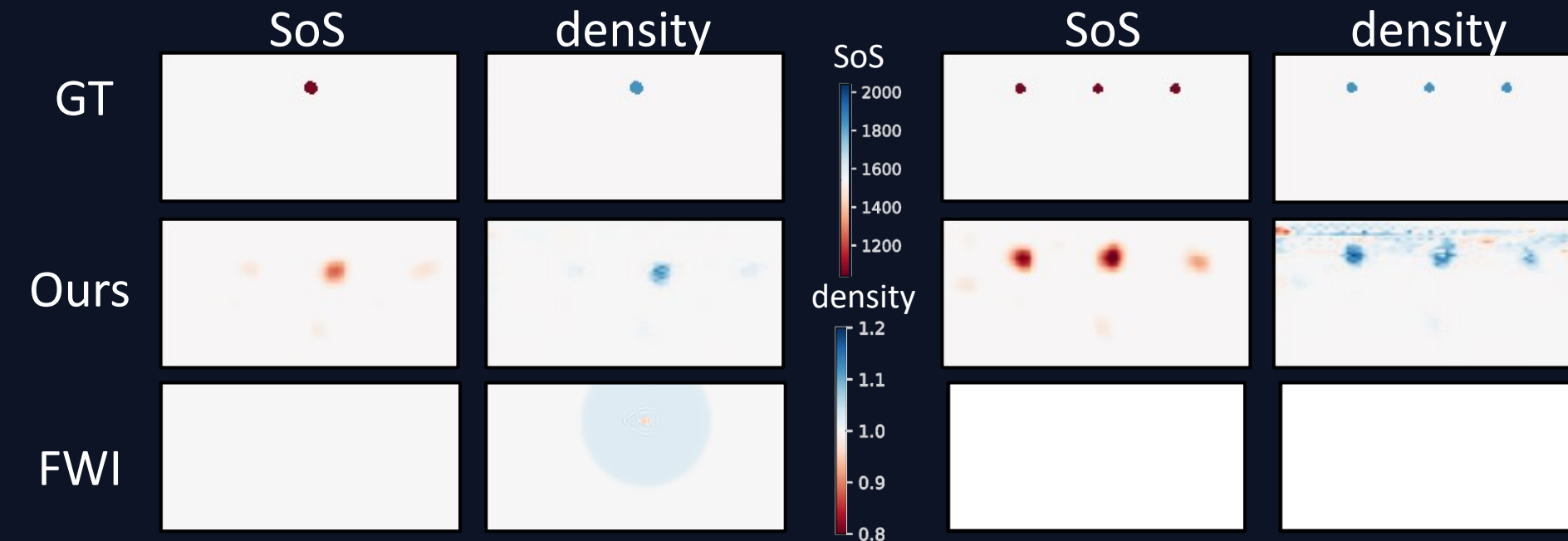


Property	NRMSE	PSNR	SSIM
conductivity	-83.53%	24.61%	1150.35%
permittivity	-79.72%	3.91%	467.33%

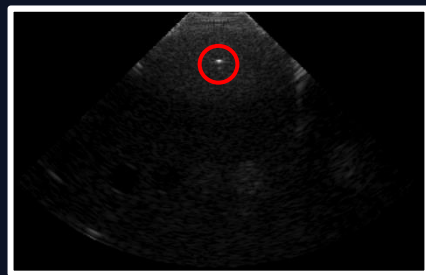
OURS	FWI
< 0.3 seconds	13-32 minutes



Phantom1 **Real Data** Phantom2



B-mode



Contribution summary

- ✓ Quantitative results in real time
- ✓ Multiple physical properties reconstruction
- ✓ Works on realistic data with high accuracy results + real recorded data
- ✓ Using data from only 8 elements
- ✓ Suitable for diverse transmission setups including linear probe
- ✓ Reconstruction from either radar or US signals

