



IMVC 2024

**Regularization-free  
Diffeomorphic Temporal  
Alignment Nets**

Ron Shapira Weber and Oren Freifeld

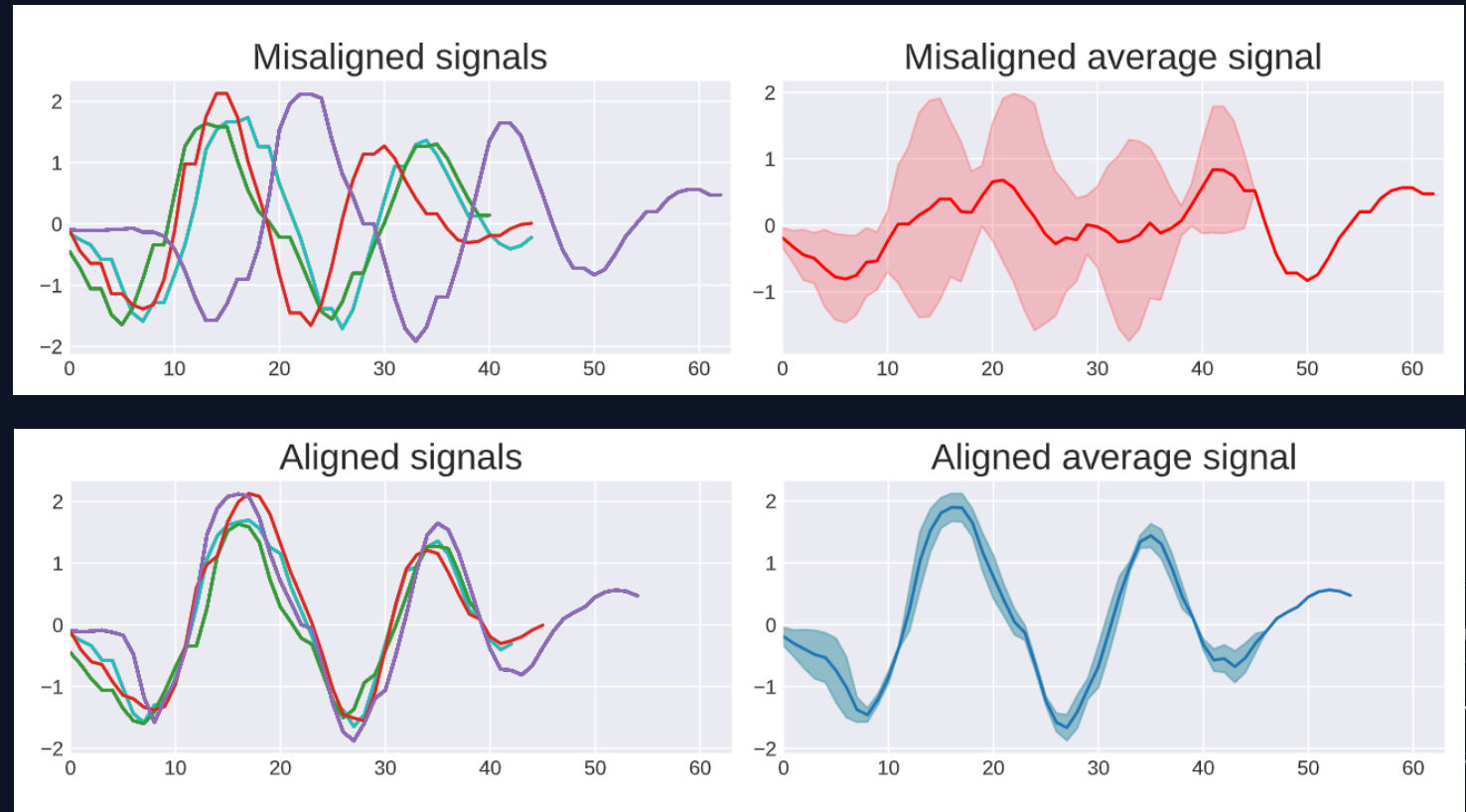
# Multiple Video synchronization w/o a reference (work in progress)



# Problem Formulation – Time Series

## Joint Alignment

Problem: nonlinear misalignment of the data



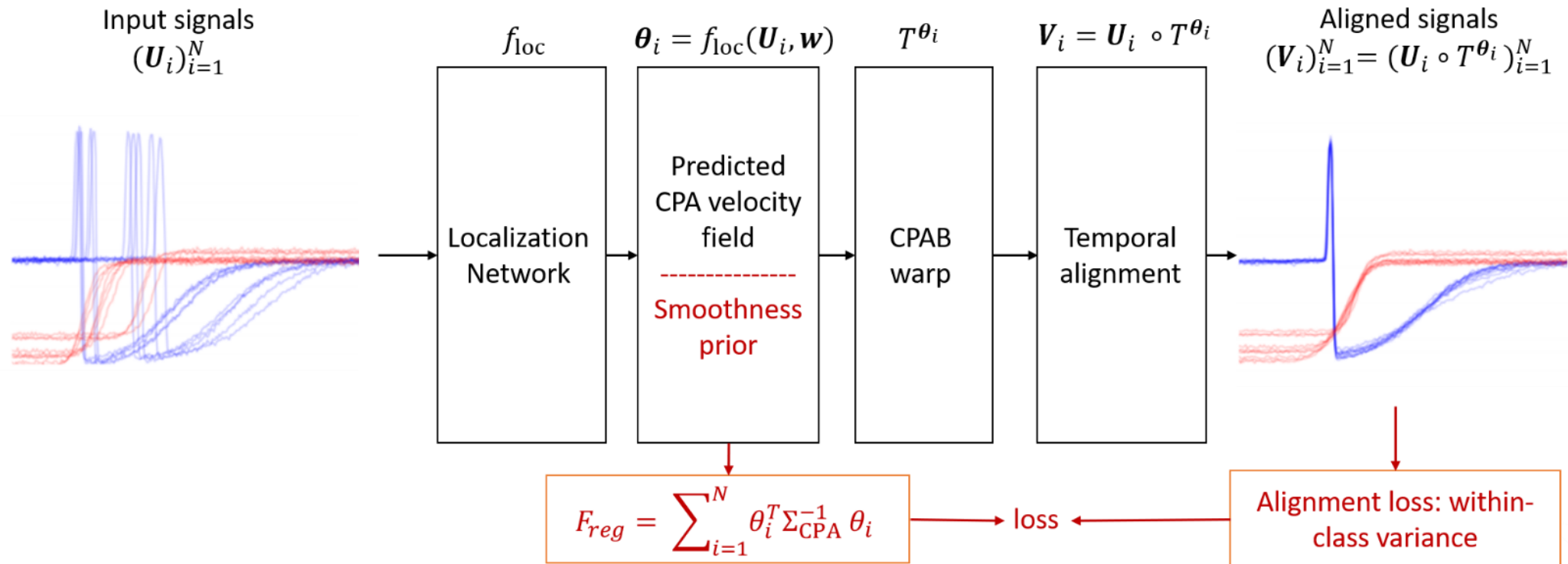
# Regularization-free Diffeomorphic Temporal Alignment Nets

- Our proposed solution –

Regularization-free Diffeomorphic Temporal Alignment Nets – RF-DTAN

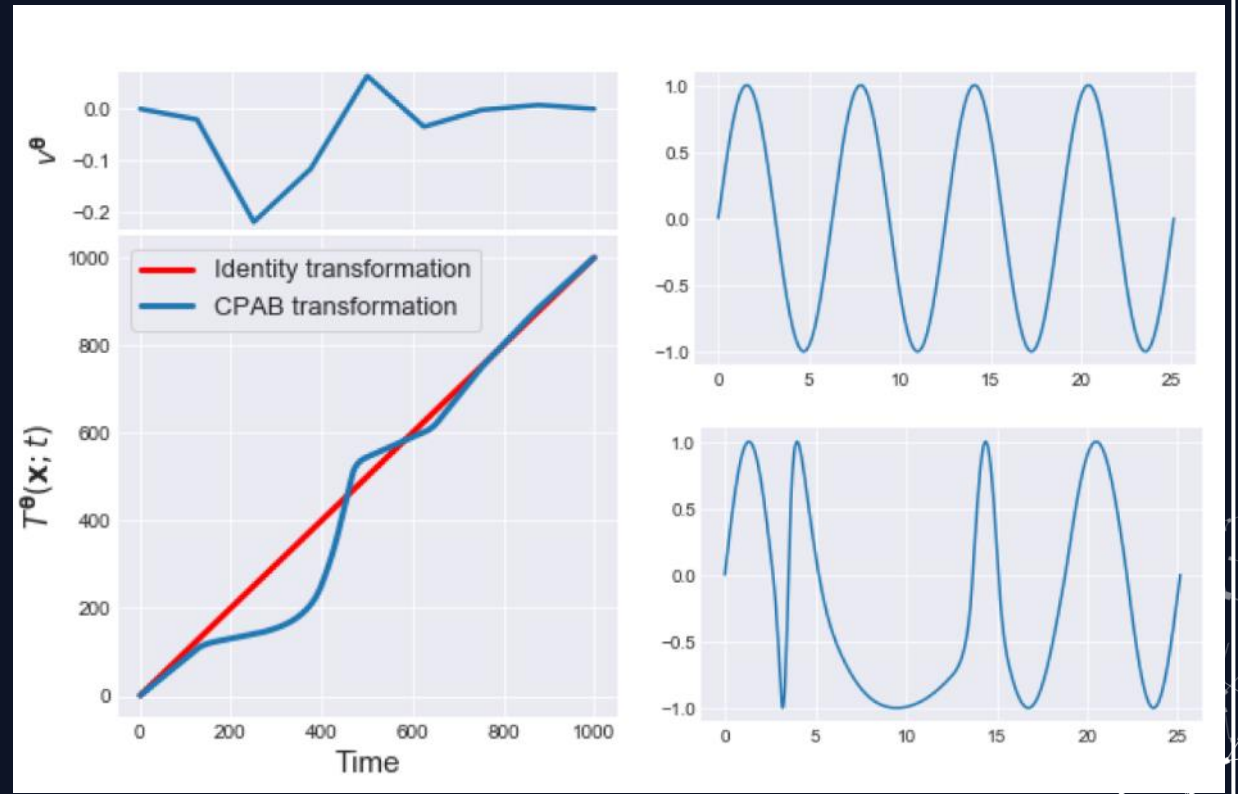
- Shapira Weber, Eyal, Skaftø Detlefsen, Shriki and Freifeld [NeurIPS '19]
- Kaufman, Shapira Weber and Freifeld [ICIP '21]
- Shapira Weber and Freifeld [ICML '23]

## DTAN (2019)



# CPAB Warps

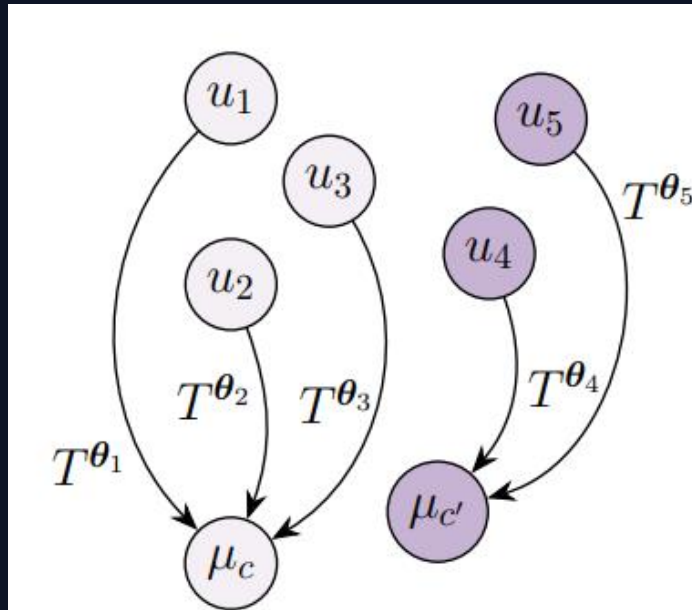
- CPAB warps [Freifeld et al., ICCV '15 & PAMI '17]
- Fast and has a closed form
- Parametric (and finite-dimensional)
- Highly-accurate & Expressive
- The gradient w.r.t. the parameters has a closed form and is fast to compute [Martinez ICML '22].



# Regularization



## DTAN (2019)



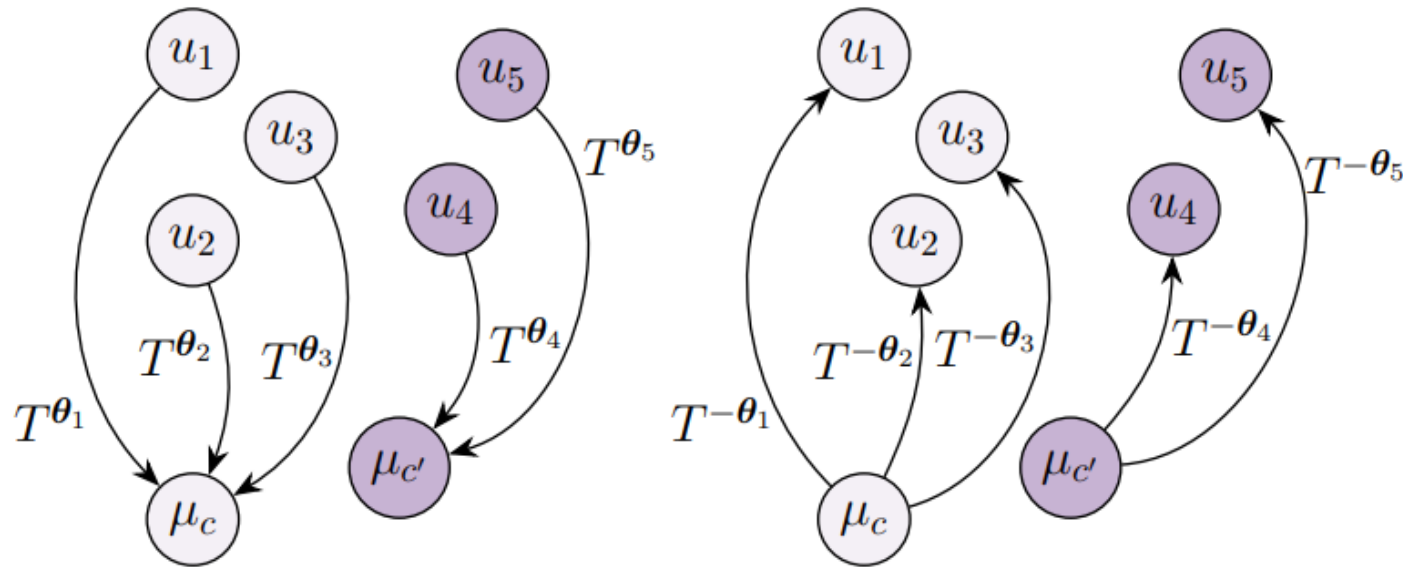
(a) Centroids computed using forward warps

$$F_{data} = \sum_{k=1}^K \frac{1}{N_k} \sum_{i:y_i=k} \|u_i \circ T^{\theta_i} - \mu_k\|_{\ell_2}^2$$

$$F_{reg} = \theta_i^T \Sigma_{CPA}^{-1} \theta_i, \text{ has 2 hyper-parameters (HP)}$$



## Regularization-free DTAN (ICML 2023)



(a) Centroids computed using forward warps

(b) The ICAE loss computed using backward warps

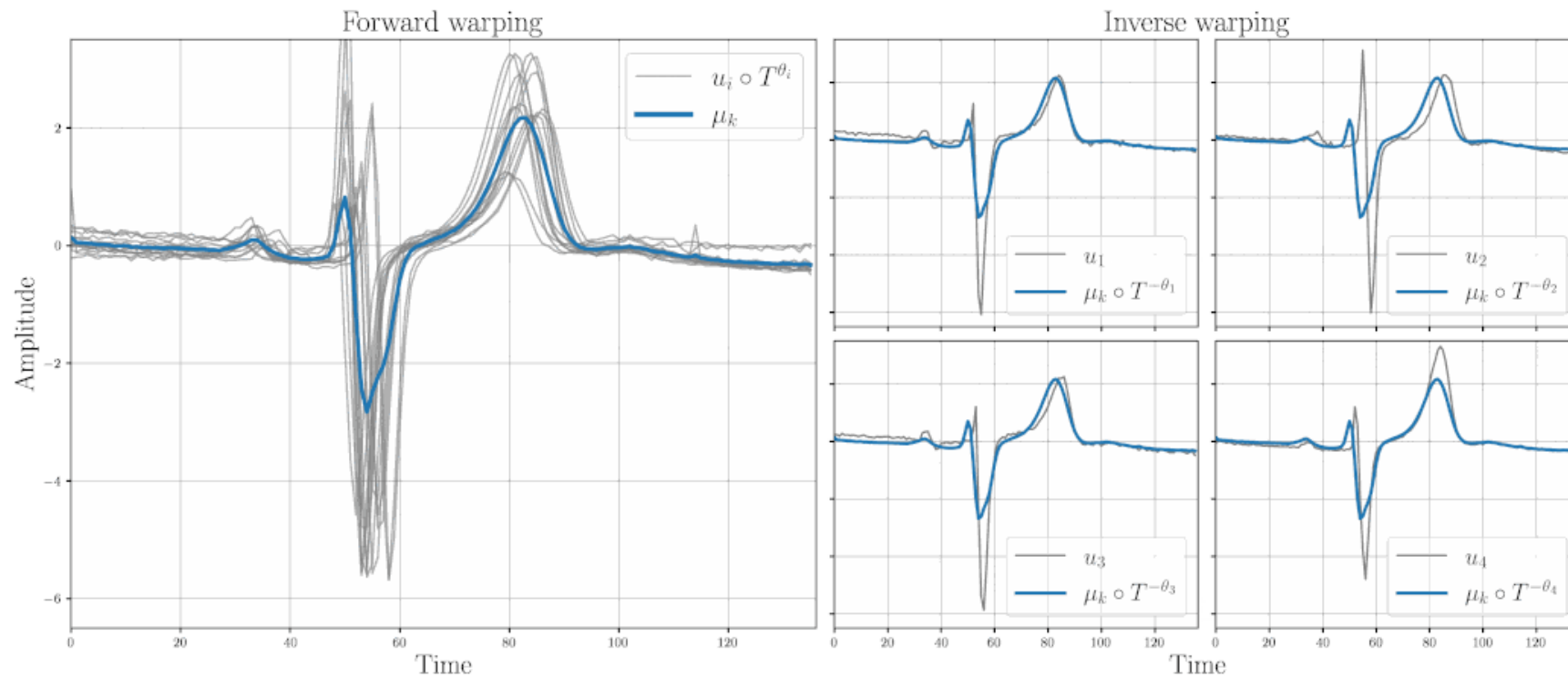
$$F_{ICAE} =$$

$$\sum_{k=1}^K \frac{1}{N_k} \sum_{i:y_i=k} \|\mu_k \circ T^{\theta_i} - u_i\|_{\ell_2}^2$$

Inverse Consistency Averaging Error (ICAE)

# Training

Inverse Consistent Averaging - Epoch 1





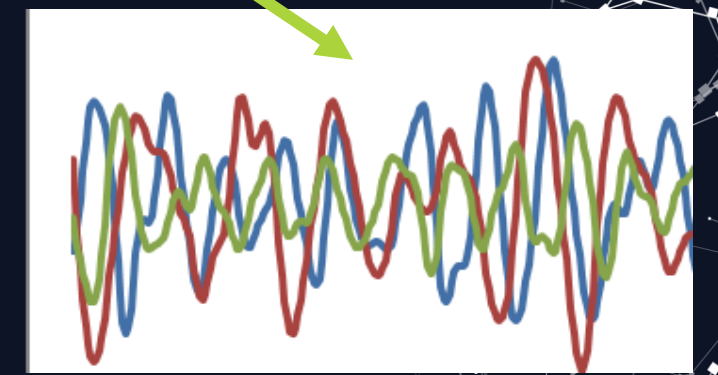
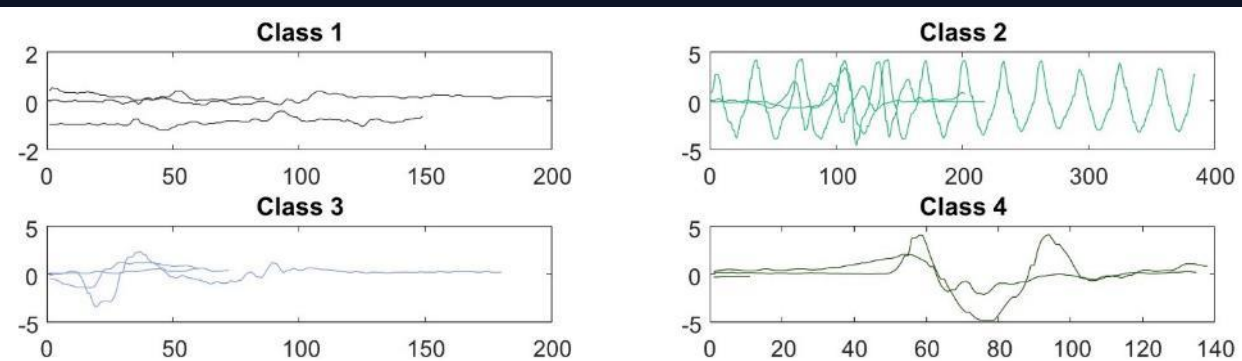
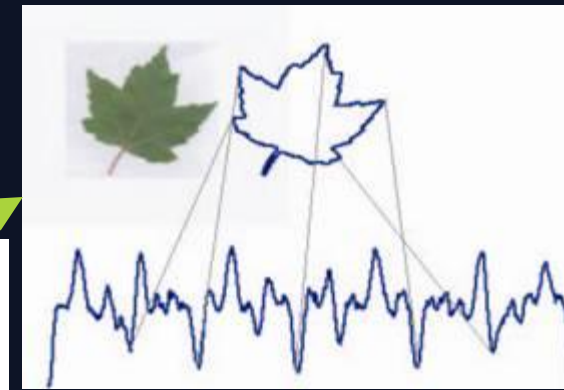
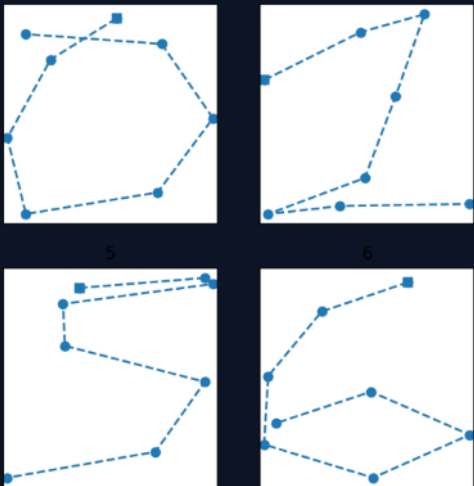
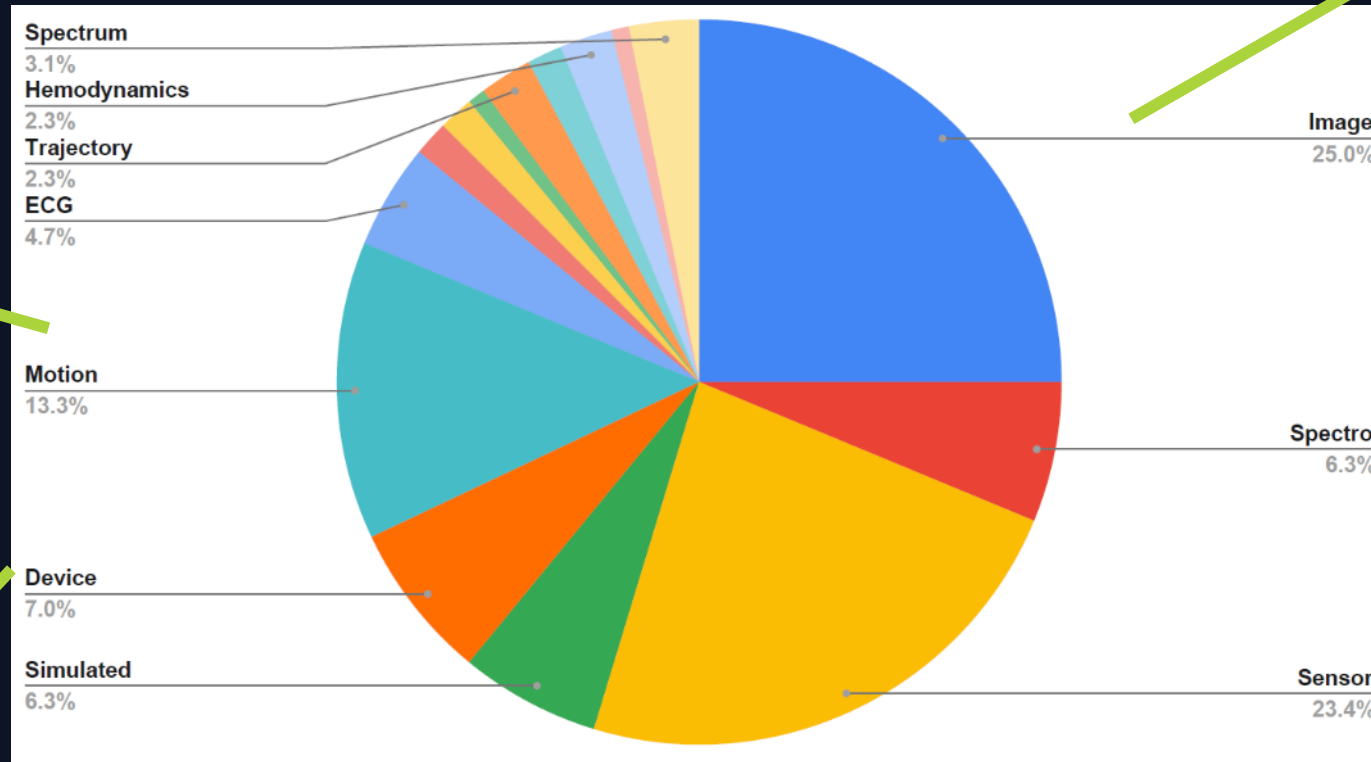
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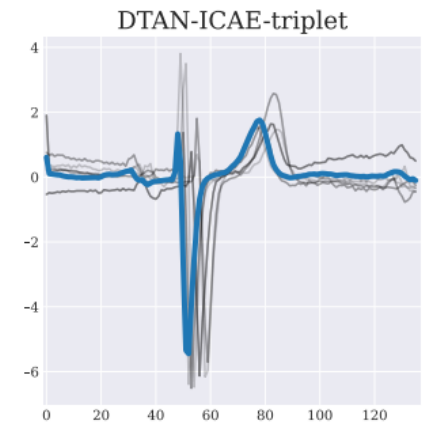
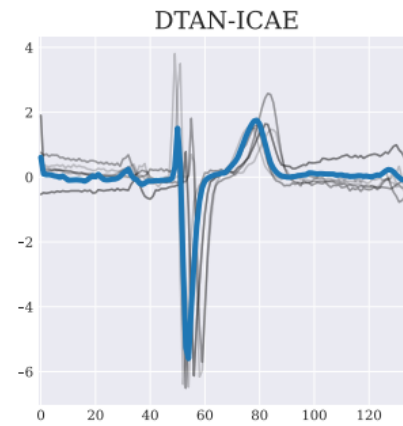
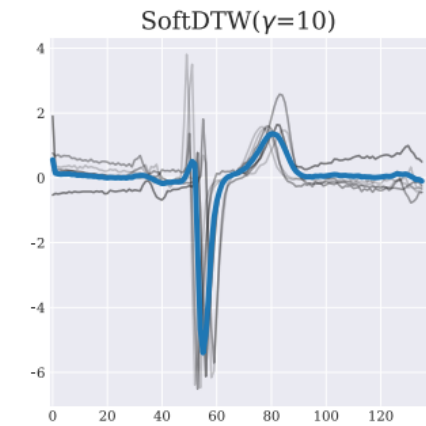
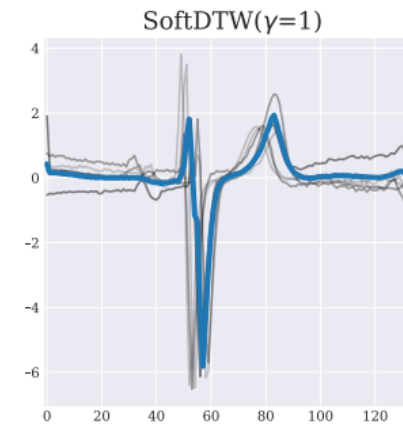
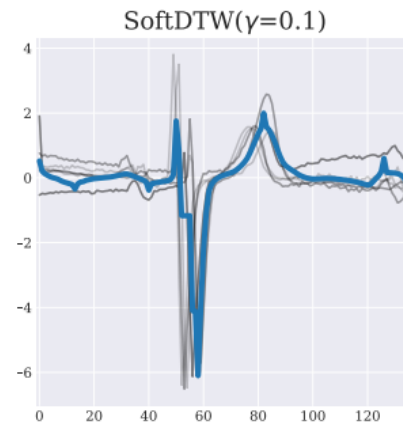
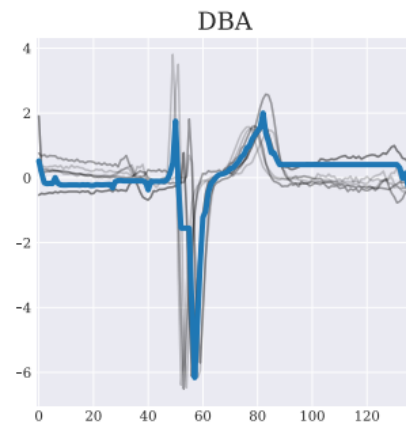
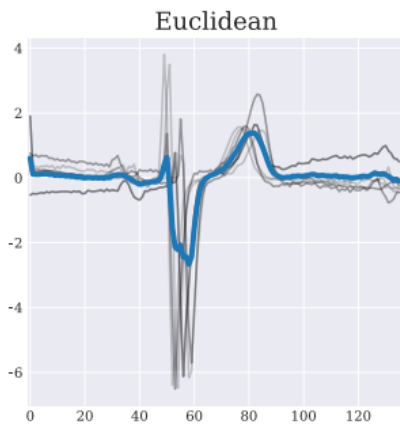
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# Results



# UCR Archive – 128 datasets [Dau et al. 2019]





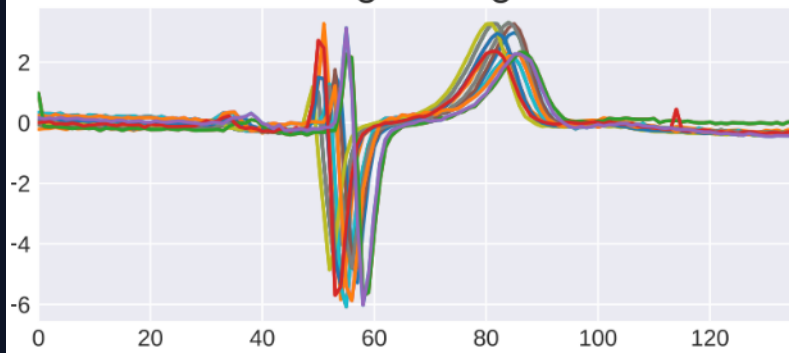


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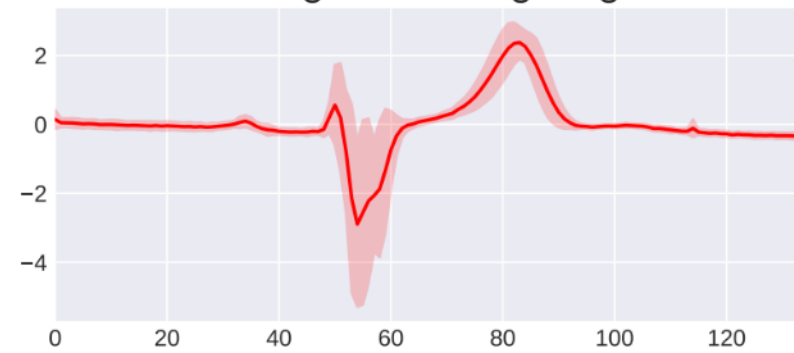
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# Results

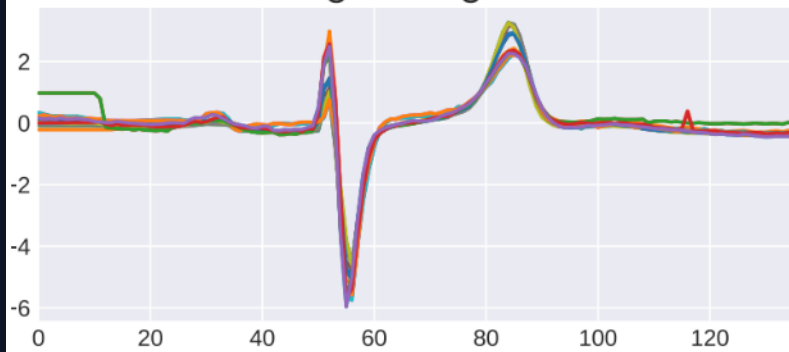
Misaligned signals



Misaligned average signal



Aligned signals



Aligned average signal

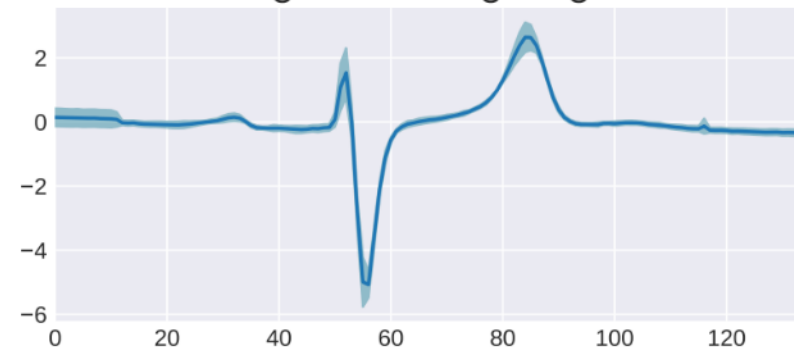
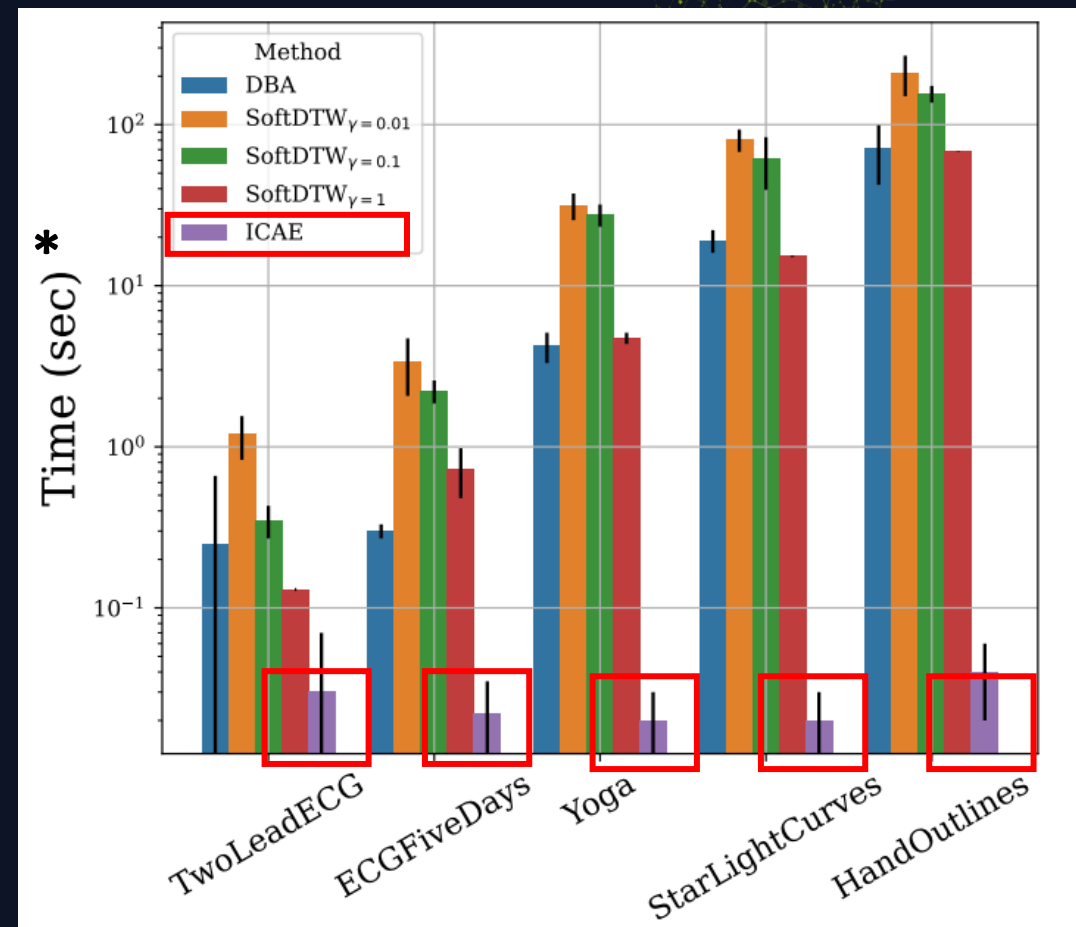


Table 2. Nearest Centroid Classification Accuracy.

METHOD	OBJECTIVE	$NCC_{\text{median}}$	$NCC_{\text{best}}$	#CONFIGS	#DATASETS	#EXPERIMENTS
PART 1: ALLOWING HP SEARCH (PREVIOUSLY-REPORTED RESULTS)						
EUCLIDEAN	N/A	-	0.611	1	84	84
DBA	DTW	-	0.657	1	84	84
SOFTDTW	SOFTDTW	-	0.703	9	84	756
SOFTDTW	SOFTDTW-DIV	-	0.708	9	84	756
DTAN <sub>libcpab</sub>	WCSS + REG	-	0.705	12	84	1008
RESNET-TW	WCSS + REG	-	0.711	20	84	1680
DTAN <sub>DIFW</sub>	WCSS + REG	-	<b>0.749</b>	96	84	8064
PART 2: SINGLE HP CONFIGURATION IN ALL DATASETS (SAME UCR DATASETS AS REPORTED BY OTHER WORKS ABOVE)						
DTAN <sub>DIFW</sub>	WCSS + REG	0.604	0.607	1	84	84
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE}}$ (OURS)	0.665	0.694	1	84	84
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE-triplet}}$ (OURS)	<b>0.707</b>	<b>0.739</b>	1	84	84
PART 3: SINGLE HP CONFIGURATION IN ALL DATASETS (INCLUDING ADDITIONAL NEWER FIXED-LENGTH UCR DATASETS)						
DTAN <sub>DIFW</sub>	WCSS	0.609	0.65	1	117	117
DTAN <sub>DIFW</sub>	WCSS + REG	0.603	0.605	1	117	117
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE}}$ (OURS)	0.656	0.686	1	117	117
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE-triplet}}$ (OURS)	<b>0.709</b>	<b>0.741</b>	1	117	117
PART 4: SINGLE HP CONFIGURATION IN ALL DATASETS (FULL UPDATED UCR ARCHIVE, INCLUDING VARIABLE-LENGTH DATASETS)						
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE}}$ (OURS)	0.623	0.653	1	128	128
DTAN <sub>DIFW</sub>	$\mathcal{L}_{\text{ICAE-triplet}}$ (OURS)	<b>0.67</b>	<b>0.701</b>	1	128	128

# Barycenter computation during inference



\*Log-scaled

Smallest  $\xrightarrow{\text{Dataset Size}}$  Largest



## Conclusion

- Goal: A system that jointly aligns a large time-series ensemble.
- Problem #1: temporal misalignment confounds statistical analysis.
- Problem #2: regularization is class/dataset-specific and requires extensive HP tuning.
- Our proposed solution: Regularization-free DTAN, variable-length alignment [ICML '23]
- Our code is publicly available at: <https://github.com/BGU-CS-VIL/RF-DTAN>



Thank you!

